

Hall Ticket Number:

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Code No. : 12221 AS N

VASAVI COLLEGE OF ENGINEERING (AUTONOMOUS), HYDERABAD

Accredited by NAAC with A++ Grade

B.E. II-Semester Advanced Supplementary Examinations, September-2023

Differential Equations &amp; Linear Algebra

(Common to CSE, AIML &amp; IT)

Time: 3 hours

Max. Marks: 60

Note: Answer all questions from Part-A and any FIVE from Part-B

Part-A (10 × 2 = 20 Marks)

| Q. No.                           | Stem of the question   | M | L | CO | PO     |
|----------------------------------|--|---|---|----|--------|
| 1.                               | Define i) Exact Differential Equation and ii) Integrating Factor   | 2 | 1 | 1  | 1,2,12 |
| 2.                               | Under what condition the differential equation $(x + x^8 + ay^2)dx + (y^8 - y + bxy)dy = 0$ becomes exact?   | 2 | 2 | 1  | 1,2,12 |
| 3.                               | Write the general solution of $(D^4 - a^4)y = 0$ .   | 2 | 2 | 2  | 1,2,12 |
| 4.                               | Write the differential equation governing L-C-R circuit.   | 2 | 1 | 2  | 1,2,12 |
| 5.                               | Write the Standard Basis for i) Vector Space of Polynomials, $P_n$ and ii) Vector Space of matrices of order $2 \times 2$ , $M_{2 \times 2}$ .   | 2 | 1 | 3  | 1,2,12 |
| 6.                               | Define Linear Dependence and Independence of vectors.  | 2 | 1 | 3  | 1,2,12 |
| 7.                               | Define Linear Transformation.  | 2 | 1 | 4  | 1,2,12 |
| 8.                               | If $T: P_4 \rightarrow P_3$ is a Linear Transformation defined by $T(p(x)) = p'(x)$ then determine the Null Space.   | 2 | 2 | 4  | 1,2,12 |
| 9.                               | Define Rank of a matrix.   | 2 | 1 | 5  | 1,2,12 |
| 10.                              | State Triangle Inequality.   | 2 | 1 | 5  | 1,2,12 |
| <b>Part-B (5 × 8 = 40 Marks)</b> |  |   |   |    |        |
| 11. a)                           | Define i) General solution and ii) Singular solution of a differential equation  | 2 | 1 | 1  | 1,2,12 |
| b)                               | Find the general and singular solution of the Clairaut's equation $y = xy' - \left(\frac{1}{y'}\right)$ .  | 6 | 3 | 1  | 1,2,12 |
| 12. a)                           | Find the Particular Integral of $(D^2 - 3D + 2)y = xe^{3x}$ .  | 3 | 3 | 2  | 1,2,12 |
| b)                               | Solve the following differential equation $(D^2 + 1)y = x \cos x$ using the method of Variation of Parameters.   | 5 | 3 | 2  | 1,2,12 |
| 13. a)                           | Define i) Subspace ii) Basis of a Vector Space iii) Dimension of a Vector Space  | 3 | 1 | 3  | 1,2,12 |
| b)                               | If W is a subspace of $M_{2 \times 2}$ of matrices with trace equal to 0, and if $S = \left\{ \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}, \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 0 \\ 1 & 0 \end{bmatrix} \right\}$ then show that S is a basis for W. | 5 | 2 | 3  | 1,2,12 |

Contd... 2

|        |   |   |   |   |        |
|--------|---|---|---|---|--------|
| 14. a) | Define a mapping $T: R^2 \rightarrow R^2$ by $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} e^x \\ e^y \end{bmatrix}$ . Determine whether $T$ is a Linear Transformation.  | 3 | 2 | 4 | 1,2,12 |
| b)     | Define the Linear operator $T: R^3 \rightarrow R^3$ by $T\left(\begin{bmatrix} x \\ y \\ z \end{bmatrix}\right) = \begin{bmatrix} x \\ -y \\ z \end{bmatrix}$ .   | 5 | 2 | 4 | 1,2,12 |
| i)     | Find the matrix of Linear operator $T$ relative to the standard basis of $R^3$ .  |   |   |   |        |
| ii)    | Use the result of a) to find $T\left(\begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix}\right)$ .  |   |   |   |        |
| 15. a) | For what values of $k$ , the matrix $\begin{bmatrix} 4 & 4 & -3 & 1 \\ 1 & 1 & -1 & 0 \\ k & 2 & 2 & 2 \\ 9 & 9 & k & 3 \end{bmatrix}$ has rank 3.  | 3 | 2 | 5 | 1,2,12 |
| b)     | Let $B$ be the basis for $R^3$ given by $B = \left\{ \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}, \begin{bmatrix} -1 \\ 1 \\ 0 \end{bmatrix}, \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix} \right\}$ . Apply Gram-Schmidt's process to $B$ to find an orthonormal basis for $R^3$ using the standard inner product of $R^3$ .   | 5 | 3 | 5 | 1,2,12 |
| 16. a) | Define Self-Orthogonal families. Show that the family of curves $y^2 = 4c(c + x)$ are self-orthogonal.  | 4 | 2 | 1 | 1,2,12 |
| b)     | Solve $(D^2 + 4D + 4)y = 4 \cos x + 3 \sin x$ , given that $y(0) = 1$ , $y'(0) = 0$ .   | 4 | 3 | 2 | 1,2,12 |
| 17.    | Answer any <i>two</i> of the following:   |   |   |   |        |
| a)     | If $W = \left\{ \begin{bmatrix} k \\ k+1 \end{bmatrix} / k \in R \right\}$ is a subset of the Vector Space $V = R^2$ with the standard definitions of vector addition and scalar multiplication, then determine whether $W$ is a subspace of $V$ .  | 4 | 3 | 3 | 1,2,12 |
| b)     | If $W$ is a subspace of all symmetric matrices in the vector space $M_{2 \times 2}$ and if $B = \left\{ \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} \right\}$ is a Basis for $W$ then find the coordinates of $\begin{bmatrix} 2 & 3 \\ 3 & 5 \end{bmatrix}$ relative to $B$ . | 4 | 3 | 4 | 1,2,12 |
| c)     | Diagonalize the matrix $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$ using Similarity Transformation.   | 4 | 3 | 5 | 1,2,12 |

M : Marks; L: Bloom's Taxonomy Level; CO; Course Outcome; PO: Programme Outcome

|      |                               |     |
|------|-------------------------------|-----|
| i)   | Blooms Taxonomy Level - 1     | 21% |
| ii)  | Blooms Taxonomy Level - 2     | 32% |
| iii) | Blooms Taxonomy Level - 3 & 4 | 47% |

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